

A psychologist studied the number of puzzles subjects were able to solve in a five-minute period while listening to soothing music. Let X be the number of puzzles completed successfully by a subject. X had the following distribution:

X	1	2	3	4
Probability	0.2	0.4	0.3	0.1

- Using the above data, what is the probability that a randomly chosen subject completes at least 3 puzzles in the five-minute period while listening to soothing music?
 - 0.3
 - 0.4
 - 0.6
 - 0.9
 - The answer cannot be computed from the information given.
- Using the above data, $P(X < 3)$ is
 - 0.3
 - 0.4
 - 0.6
 - 0.9
 - The answer cannot be computed from the information given.
- Using the above data, the mean μ of X is
 - 2.0
 - 2.3
 - 2.5
 - 3.0
 - The answer cannot be computed from the information given.
- Which of the following random variables should be considered continuous?
 - The time it takes for a randomly chosen woman to run 100 meters
 - The number of brothers a randomly chosen person has
 - The number of cars owned by a randomly chosen adult male
 - The number of orders received by a mail order company in a randomly chosen week
 - None of the above

5. A dealer in the Sands Casino in Las Vegas selects 40 cards from a standard deck of 52 cards. Let Y be the number of red cards (hearts or diamonds) in the 40 cards selected. Which of the following best describes this setting:
- (a) Y has a binomial distribution with $n = 40$ observations and probability of success $p = 0.5$.
 - (b) Y has a binomial distribution with $n=40$ observations and probability of success $p = 0.5$, provided the deck is shuffled well.
 - (c) Y has a binomial distribution with $n=40$ observations and probability of success $p = 0.5$, provided after selecting a card it is replaced in the deck and the deck is shuffled well before the next card is selected.
 - (d) Y has a normal distribution with mean $p = 0.5$.
6. In a certain large population, 40% of households have a total annual income of over \$70,000. A simple random sample is taken of 4 of these households. Let X be the number of households in the sample with an annual income of over \$70,000 and assume that the binomial assumptions are reasonable. What is the mean of X ?
- (a) 1.6
 - (b) 28,000
 - (c) 0.96
 - (d) 2, since the mean must be an integer
 - (e) The answer cannot be computed from the information given.
7. The probability that a three-year-old battery still works is 0.8. A cassette recorder requires four working batteries to operate. The state of batteries can be regarded as independent, and four three-year-old batteries are selected for the cassette recorder. What is the probability that the cassette recorder operates?
- (a) 0.9984
 - (b) 0.8000
 - (c) 0.5904
 - (d) 0.4096
 - (e) The answer cannot be computed from the information given.
8. Twenty percent of all trucks undergoing a certain inspection will fail the inspection. Assume that trucks are independently undergoing this inspection, one at a time. The expected number of trucks inspected before a truck fails inspection is
- (a) 2
 - (b) 4
 - (c) 5
 - (d) 20
 - (e) The answer cannot be computed from the information given.

Chapter 7/8 Practice Free Response

9. A box contains ten \$1 bills, five \$2 bills, three \$5 bills, one \$10 bill, and one \$100 bill. A person is charged \$20 to select one bill. Define the random variable X as the amount on the random bill.
- Construct the probability distribution for X .
 - Find the expected value for X .
 - Taking into account that it costs \$20 to play this game, is the game fair? Explain.
10. Amarillo Slim, a professional dart player, has an 80% chance of hitting the bullseye on a dartboard with any throw. Suppose that he throws 10 darts, one at a time, at the dartboard.
- Find the probability that Slim hits the bullseye exactly six times.
 - Find the probability that he hits the bullseye at least four times.
 - Compute the mean of the number of bullseyes in 10 throws.
 - Find the probability that Slim's first bullseye occurs on the fourth throw.
 - Find the probability that it takes Amarillo more than 2 throws to hit the bullseye.
11. Harlan comes to class one day, totally unprepared for a pop quiz consisting of ten multiple-choice questions. Each question has five answer choices, and Harlan answers each question randomly.
- Find the probability that Harlan guesses more answers correctly than would be expected by chance.
 - Find the probability that Harlan's first correct answer occurs on or after the fourth question.

Answers to the Review for Chapters 7 and 8

Multiple Choice

Chapter 7

1. b 2. c 3. b 4. a

Chapter 8

5. c 6. a 7. d 8. c

Free Response

9. A box contains ten \$1 bills, five \$2 bills, three \$5 bills, one \$10 bill, and one \$100 bill. A person is charged \$20 to select one bill. Define the random variable X as the amount on the random bill.

(a)

X	\$1	\$2	\$5	\$10	\$100
P(X)	.5	.25	.15	.05	.05

(b) $\mu_x = \$1(.5) + \$2(.25) + \$5(.15) + \$10(.05) + \$100(.05) = \7.25

(c) No it is not fair; you stand to lose way too much money every time you play. The expected return per play is $\$7.25 - \$20.00 = -\$12.75$. So you will lose \$12.75 per play, on average.

10. Amarillo Slim, a professional dart player, has an 80% chance of hitting the bullseye on a dartboard with any throw. Suppose that he throws 10 darts, one at a time, at the dartboard.

(a) *Binomial*: $P(X = 6) = \frac{10!}{6!4!} (.8)^6 (.2)^4 = .088$.

(b) *Binomial*: $P(X \geq 1) = 1 - P(X \leq 3) = 1 - \text{binomcdf}(10, .8, 3) = .999$.

(c) *Binomial*: $\mu = np = 10(.8) = 8$.

(d) *Geometric*: $P(X = 4) = (.2)^3 (.8) = .0064$.

(e) *Geometric*: $P(X > 2) = (.2)^2 = .04$.

11. Harlan comes to class one day, totally unprepared for a pop quiz consisting of ten multiple-choice questions. Each question has five answer choices, and Harlan answers each question randomly.

(a) *Binomial* expected = $np = 10(.2) = 2$. So we are looking for the probability that $X > 2$.

$$P(X > 2) = 1 - P(X \leq 2) = 1 - \text{binomcdf}(10, .2, 2) = .624.$$

(b) *Geometric*: $P(X > 3) = (.8)^3 = .512$.